

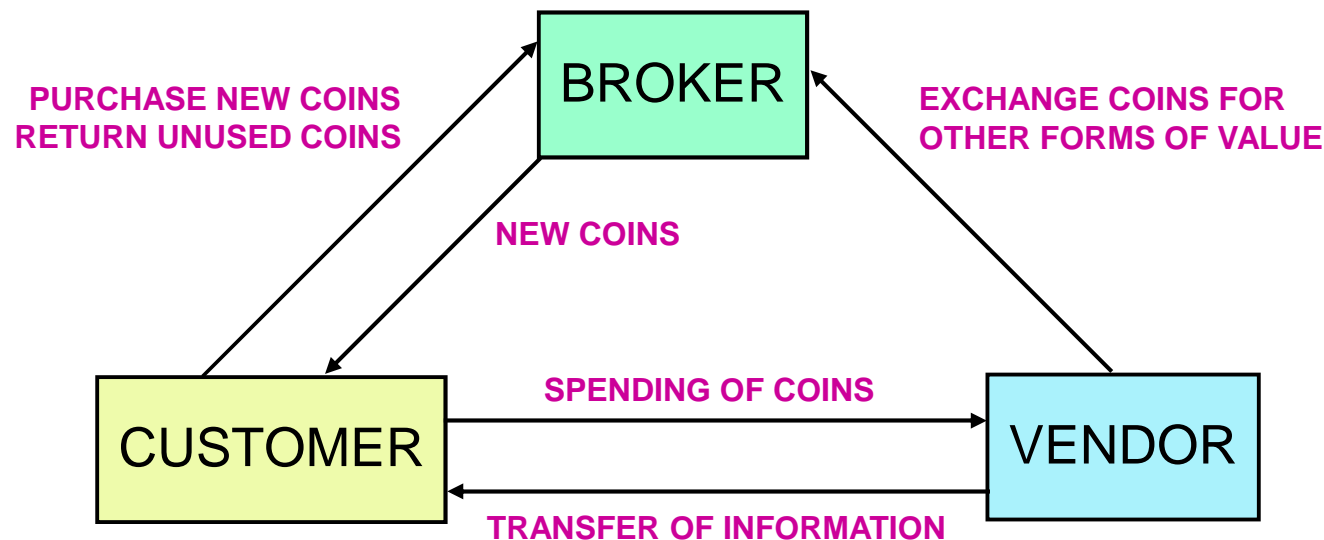
# **Electronic Payment Systems 20-763**

## **Lecture 9: Micropayments II**



# MicroMint

- Brokers produce “coins” having short lifetimes, sell coins to users
- Users pay vendors with coins
- Vendors exchange the coins with brokers for “real” money



SOURCE: SHERIF

# Minting Coins in MicroMint

- Idea: make coins easy to verify, but difficult to create (so there is no advantage in counterfeiting)
- In MicroMint, coins are represented by hash-function collisions, values  $x, y$  for which  $H(x) = H(y)$
- If  $H(\bullet)$  results in an  $n$ -bit hash, we have to try about  $2^{n/2}$  values of  $x$  to find a first collision
- Trying  $c \cdot 2^{n/2}$  values of  $x$  yields about  $c^2$  collisions
- Collisions become cheaper to generate after the first one is found

# Coins as k-way Collisions

- A k-way collision is a set  $\{ x_1, x_2, \dots, x_k \}$  with
$$H(x_1) = H(x_2) = \dots = H(x_k)$$
- It takes about  $2^{n(k-1)/k}$  values of  $x$  to find a k-way collision
- Trying  $c \cdot 2^{n(k-1)/k}$  values of  $x$  yields about  $c^k$  collisions
- If  $k > 2$ , finding a first collision is slow, but subsequent collisions come fast
- If a k-way collision  $\{ x_1, x_2, \dots, x_k \}$  represents a coin, easily verified by computing  $H(x_1), H(x_2), \dots, H(x_k)$
- A broker can easily generate 10 billion coins per month using one machine

# Selling MicroMint Coins

- Broker generates 10 billion coins and stores  $(x, H(x))$  for each coin, having a validity period of one month
- The function  $H$  changes at the start of each month
- Broker sells coins  $\{ x_1, x_2, \dots, x_k \}$  to users for “real” money, records who bought each coin
- At end of month, users return unused coins for new ones

# Spending MicroMint Coins

- User sends vendor a coin  $\{ x_1, x_2, \dots, x_k \}$
- Vendor verifies validity by checking that  $H(x_1) = H(x_2) = \dots = H(x_k)$ . (k hash computations)
- Valid but double-spent coins (previously used with a different vendor) cannot be detected at this point
- At end of day, vendor sends coins to broker
- Broker verifies coins, checks validity, checks for double spending, pays vendor
- (Need to deal with double spending at this point)

# Detecting MicroMint Forgery

- A forged coin is a  $k$ -way collision  $\{ x_1, x_2, \dots, x_k \}$  under  $H(\bullet)$  that was not minted by broker
- Vendor cannot determine this in real-time
- Small-scale forgery is impractical
- Forged coins become invalid after one month
- New forgery can't begin before new hash is announced
- Broker can issue recall before the month ends
- Broker can stay many months ahead of forgers

# Statistical Schemes

- During World War II, Cola-Cola raised the price of a bottle from 5 cents (\$0.05) to 6 cents (\$0.06)
- It was expensive to change the coin mechanism
- Coca-Cola randomly removed 1/5 of the bottles from its machines but kept the 5-cent mechanism
- 4/5 of the time a customer would receive a bottle for 5 cents
- 1/5 of the time a customer would pay 5 cents and get NOTHING
- The AVERAGE price of a bottle was 6 cents
- Rarely, a user might pay a lot for a bottle (1 in 625 bottles cost 20 cents)



# Statistical Payment



User needs to pay Mapquest \$0.01

**MAPQUEST.**



McDonald's  
965 Edwards Ferry Rd  
Leesburg, VA 20176  
(703-7716035)  
About 2 miles  
NEXT OPTN

## FAIRNESS:

- User, merchant and bank cannot cheat
- Not always fair to user (might be overcharged)
- Fair to merchant and bank on average

1/1000

999/1000

**\$10**

**VOID**



Enable 1000 Transactions  
at Cost of 1

# MR1 (Micali, Rivest)

- Three parties: user U, merchant M, bank B
- For simplicity, assume every transaction is worth \$0.01 but we only want to process transactions with probability  $1/1000$
- U and M have public-private key pairs
- Let F be a publicly available function (everyone can obtain the code) that returns a number between 0 and 1 uniformly. (The values of F are uniformly distributed between 0 and 1.)
- A transaction string  
$$T = \text{User ID} \parallel \text{Merchant ID} \parallel \text{Bank ID} \parallel \text{timestamp}$$

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SOURCE: RON RIVEST

# MR1, continued

- When User U wants to pay Merchant M, he sends M his digital signature C for transaction string T
$$C = \text{Sig}_U(T) \quad (\text{hash of } T \text{ encrypted with } U\text{'s private key})$$
- Merchant M now signs C
$$D = \text{Sig}_M(C) \quad (\text{hash of } C \text{ encrypted with } M\text{'s private key})$$
- Merchant M computes  $F(D)$ 
  - If  $F(D) < .001$ , then C is worth \$10; otherwise C is worth \$0
  - This occurs 1/1000 of the time
- If C has value, M sends to bank C &  $D = \text{Sig}_M(C)$
- Bank verifies signatures and  $F(D)$ , charges U \$10 and credits M with \$10
- No risk to bank; U may pay a lot more than the transaction value

SOURCE: RON RIVEST

# Properties of MR1

- Payment is off-line
  - U and M do not have to be in contact during transaction
  - U can send C by email
  - M does not have to contact Bank during transaction
- Bank only sees 0.1% of transactions
- No risk to bank
- Because of signatures, neither U nor M can cheat (if protocol is implemented properly)
- U may pay a lot more than the transaction value
- Want a protocol in which U never pays more than the transaction value

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SOURCE: RON RIVEST

# MR2 (Micali, Rivest)

- Goal: make sure U never pays more than transaction value he uses
- Shift risk from User to Bank. This is OK because Bank processes large number of transactions
- U includes a serial number S as part of the transaction string
- Let MaxS be the highest serial number the Bank has processed for user U so far (starts at 0)
- When Bank processes a payable transaction:
  - credits M with \$10
  - debits U by  $S - \text{MaxS}$
  - $\text{MaxS} \leftarrow S$

# Why Does MR2 Work?

- User NEVER pays more than the number of transactions he creates
- After  $n$  transactions, serial number  $S = n$ . Suppose he has to pay  $m$  times
- Total payment =

$$\sum_{i=1}^m S_i - \text{Max}S_i = \sum_{i=1}^{m-1} \text{Max}S_{i+1} - \text{Max}S_i = S_m = n$$

- User can cheat (by not incrementing  $S$ ), but Bank will catch him
- Bank on average receives as much as it pay out

# Properties of MR1 and MR2

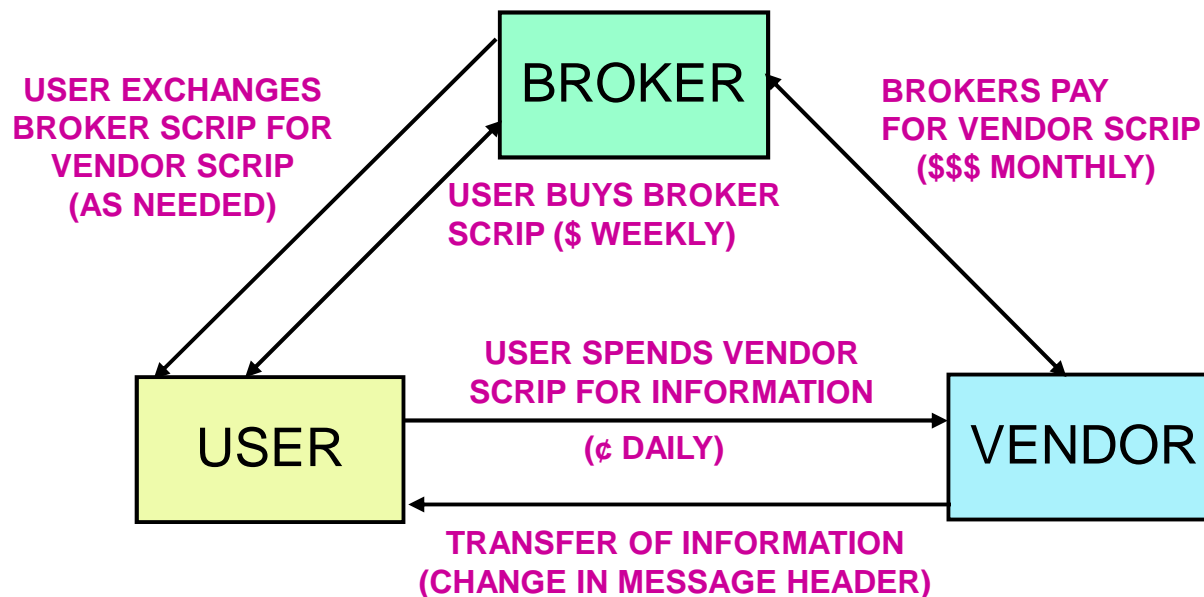
- Highly scalable: billions of transactions handled with only millions of payments
- Inexpensive
- Payments are offline
- Global aggregation (can handle payments to many merchants from many customers)

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SOURCE: RON RIVEST

# Millicent

- Vendors produce vendor-specific “scrip”, sell to brokers for “real” money at discount
- Brokers sell scrip from many vendors to many users
- Scrip is prepaid: promise of future service from vendor
- Users “spend” scrip with vendors, receive change



SOURCE: COMPAQ

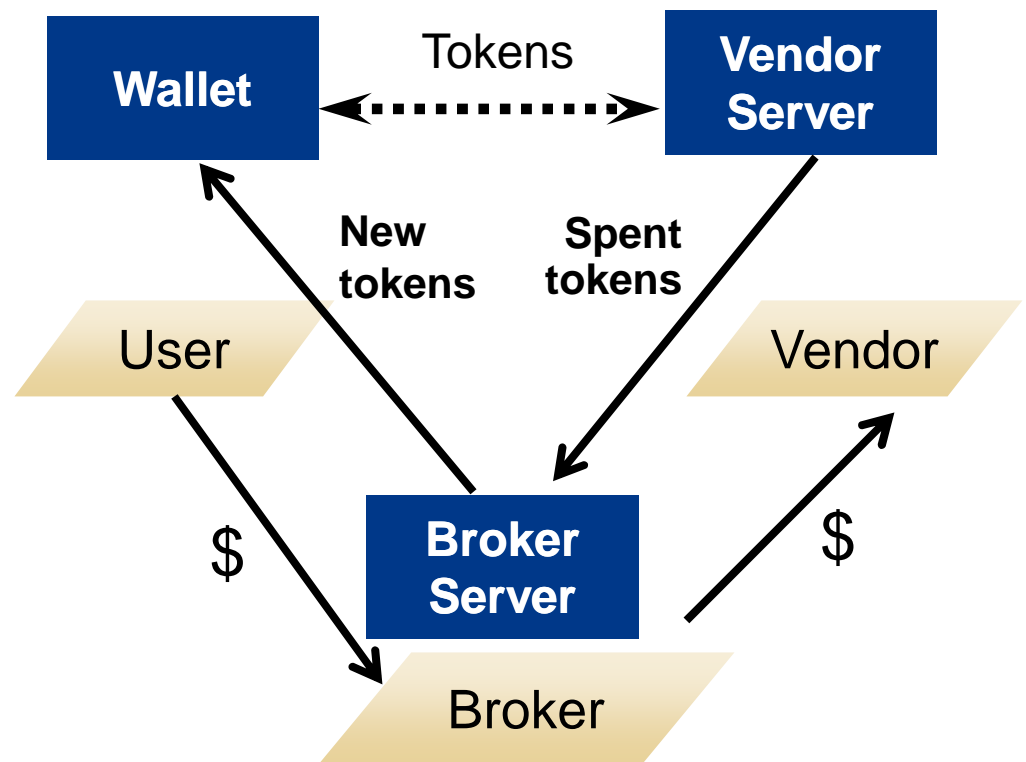


# Millicent

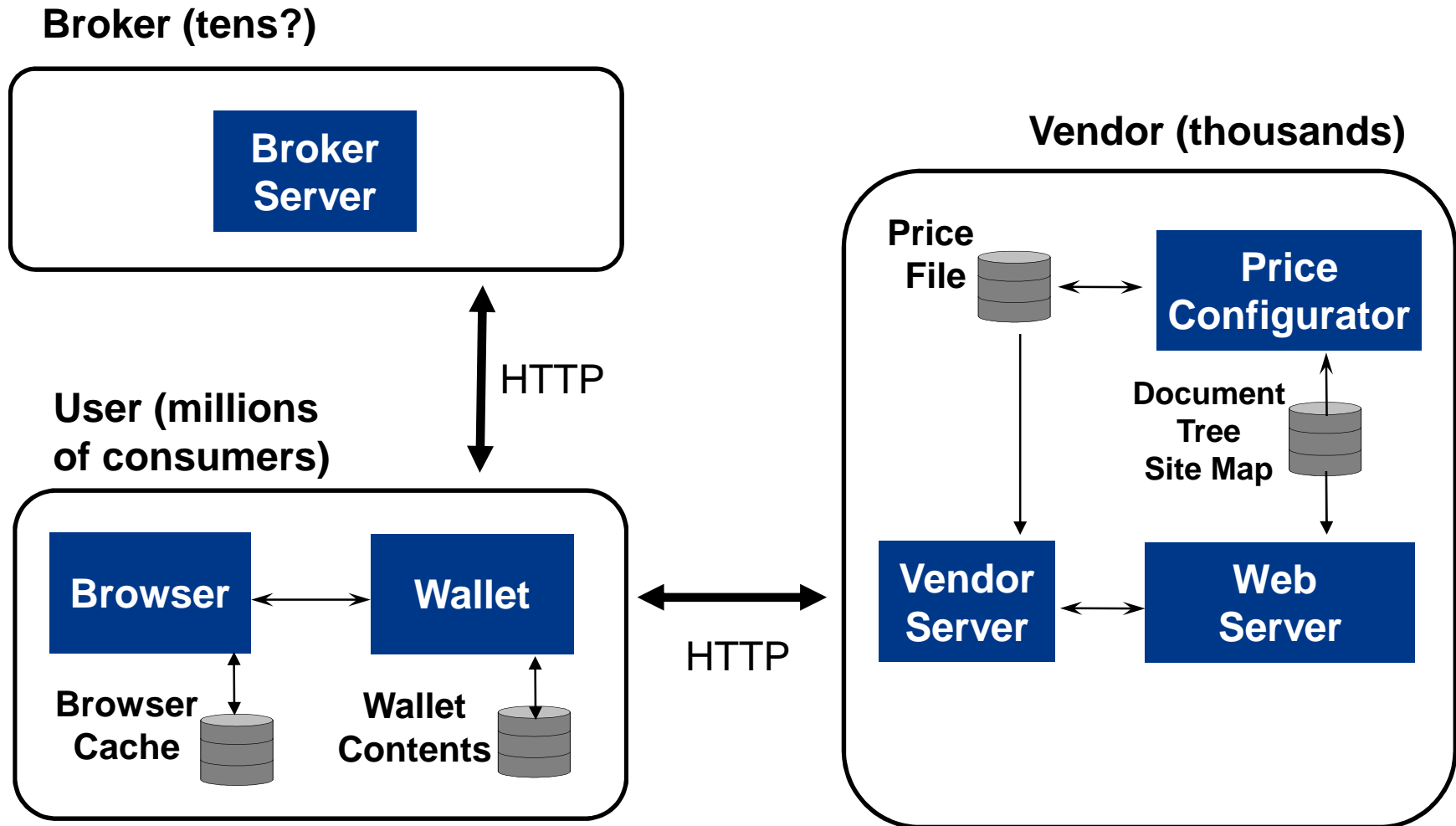
- Broker
  - issues broker scrip to user
  - exchanges broker scrip for vendor scrip
  - interfaces to banking system
  - collects funds from users
  - pays vendors (less commission)
- User
  - buys broker scrip from brokers
  - spends by obtaining vendor-specific scrip from broker
- Vendor
  - sells scrip to brokers
  - accepts vendor scrip from users
  - gives change to users in vendor scrip

# MilliCent Components

- **Wallet**
  - integrated with browser as a “proxy”
  - User Interface (content, usage)
- **Vendor software**
  - easy to integrate as a web relay
  - utility for price management
- **Broker software**
  - handles real money

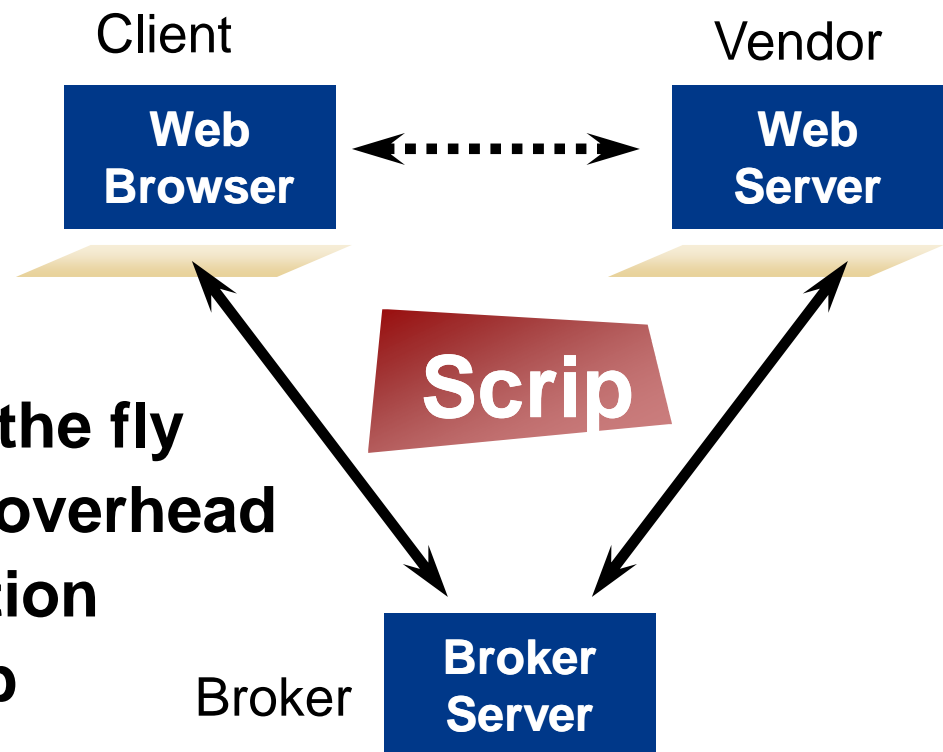


# MilliCent System Architecture



# Millicent Scrip Verification

- Token attached to HTTP requests
- **Scrip** can not be:
  - Spent twice
  - Forged
  - Stolen
- **Scrip** is validated:
  - By each vendor, on the fly
  - Low computational overhead
  - No network connection
  - No database look up



# MilliCent Scrip

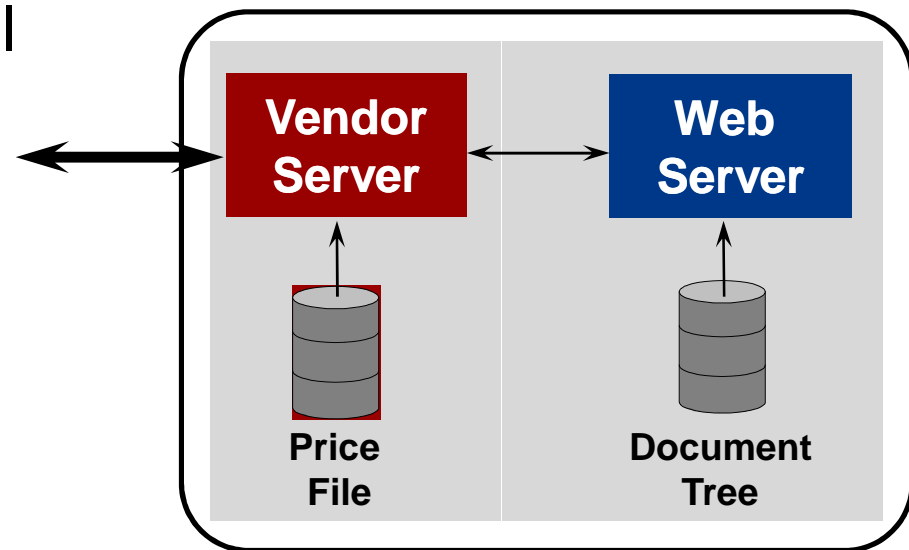


Vendor	Value	ID#	Cust ID#	Expires	Props	Stamp	Secret
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wellsfargo.com / 0.005usd / 0081432 / 101861 / 19961218 {co=us/st=ca} 1d7f4a734b7c02282e48290f04c20

# Vendor Server

- Vendor server acts as a proxy for the real Web server
- Vendor server handles all requests:
  - Millicent
  - relay to web-server
- Millicent processing:
  - Validates scrip and generates change
  - Sells subscriptions
  - Handles replays, cash-outs, and refunds



**Vendor Site**

# Major Ideas

- Micropayment systems must be fast and cheap
- They **MUST** lack features of higher-value payment systems
- Use of hashing instead of cryptography
- Micropayment parties: buyer, seller, broker
- Micromint models minting coins
  - High overhead to prevent counterfeiting
- Fraud is not a serious problem with micropayments

# Q&A